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# Molecular Orbital Studies of Electron Donor-Acceptor Complexes. 4. Energy Decomposition Analysis for Halogen Complexes: $H_3N-F_2$ , $H_3N-Cl_2$ , $H_3N-ClF$ , $CH_3H_2N-ClF$ , $H_2CO-F_2$ , HF-ClF, and $F_2-F_2$

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Abstract: The energy and charge distribution decomposition analyses are carried out for a series of electron donor-acceptor complexes of halogens. Based on the energy components essential for binding, the complexes are qualitatively classified as follows:  $H_3N-F_2$   $H_3N-Cl_2$ , and  $H_2CO-F_2$ , weak electrostatic charge transfer complexes;  $H_3N-Cl_F$ , intermediate electrostatic complex; HF-CIF, weak electrostatic complex; and  $F_2$ - $F_2$ , very weak dispersion-charge transfer complex. The energy components determining the equilibrium geometry as well as the N-methyl substituent effect are also identified, and comparisons between various complexes have been made. The predicted geometry of an anti-hydrogen bonded complex FCI-FH is in good agreement with experiment, but the hydrogen bonded counterpart CIF-HF appears to be comparable in energy. The SCF interaction energy for  $(F_2)_2$  favors an open L shape.

## I. Introduction

The origin of attractive intermolecular interactions and the factors determining the geometry of molecular complexes have been sought after for decades using numerous experimental and theoretical techniques.<sup>1,2</sup> For hydrogen bonding, which in earlier days had been considered to be a purely electrostatic interaction, the importance of the charge transfer interaction has long been emphasized.1 The electron donoracceptor (EDA) complex or the charge transfer complex was originally thought to be stabilized principally by the charge transfer interaction between the donor and acceptor molecules.<sup>2,3</sup> Later studies have suggested that many such complexes, especially weak complexes, are bound primarily due to the electrostatic and polarization interactions.<sup>4,5</sup> Since the interaction is quantum mechanical in nature, quantum chemical calculations should be able to provide substantial information regarding the nature of the binding.

The ab initio SCF molecular orbital (MO) method has been very successful in both predicting the equilibrium geometry and stabilization energy of many hydrogen bonded and EDA complexes and in interpreting the nature of such interactions.<sup>6,1b</sup> The energy and charge distribution decomposition (ECDD) analyses proposed by Morokuma<sup>7</sup> and Kitaura and Morokuma<sup>8</sup> have provided a means for direct examination of the origin of molecular interactions.<sup>9-15</sup> Using either the model wave function or model Hartree-Fock operator they unambiguously defined components of the total interaction,  $\Delta E_{SCF}$ , which are in accord with traditional viewpoints.<sup>16</sup>

The individual components have the following physical significance.17

ES is the electrostatic interaction, i.e., the interaction between the undistorted electron distribution of a monomer A and that of a monomer B. This contribution includes the interactions of all permanent charges and multipoles, such as dipole-dipole, dipole-quadrupole, etc. This interaction may be either attractive or repulsive.

PL is the polarization interaction, i.e., the effect of the distortion (polarization) of the electron distribution of A by B, the distortion of B by A, and the higher order coupling resulting from such distortions. This component includes the interactions between all permanent charges or multipoles and induced multipoles, such as dipole-induced dipole, quadrupole-induced dipole, etc. This is always an attractive interaction.

EX is the exchange repulsion, i.e., the interaction caused by exchange of electrons between A and B. More physically, this is the short-range repulsion due to overlap of electron distribution of A with that of B.

CT is the charge transfer or electron delocalization interaction, i.e., the interaction caused by charge transfer from occupied MO's of A to vacant MO's of B, and from occupied MO's of B to vacant MO's of A, and the higher order coupled interactions.

MIX is the coupling term which is the difference between the total SCF interaction energy  $\Delta E_{SCF}$  and the sum of the above four components and accounts for higher order interaction between various components.

 $\Delta E_{SCF} = ES + PL + EX + CT + MIX$ (1)

In addition to the above components calculated within the Hartree-Fock scheme, there is a contribution of the correlation

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energy  $\Delta E_{\text{corr}}$  which can further be divided into the intramolecular correlation term, CA, and the intermolecular term, CR.

$$\Delta E_{\rm corr} = CA + CR \tag{2}$$

A part of the intermolecular correlation term CR is known as the dispersion energy, DISP.<sup>16</sup> This is the interaction resulting from instantaneous polarization of A and B. Approximate calculations for atomic and molecular interactions and apparent successes of Hartree–Fock calculations indicate that the effect of  $\Delta E_{\rm corr}$  is relatively unimportant for interactions of polar molecules.

In the previous papers of this series, we have used the ECDD analysis to elucidate the origin of interaction in the ground and some lower excited states of several EDA complexes. Around the equilibrium geometry of the ground state of weak  $n-\pi^*$ complexes such as ether ROR (a so-called n-electron donor) -carbonyl cyanide OC(CN)<sub>2</sub> (a so-called  $\pi$ -electron acceptor), and ether-tetracyanoethylene  $(NC)_2C=C(CN)_2$  (a  $\pi$  acceptor), we found that the electrostatic interaction ES was the dominant contributor (several kcal/mol) to the stabilization, while the contribution of the charge transfer energy, CT, was not essential (of the order of 1 kcal/mol).<sup>12</sup> One may well call these complexes "weak electrostatic complexes". In the benzene-carbonyl cyanide complex, the dispersion energy, DISP, was found to be as important as the SCF contribution  $\Delta E_{SCF}$ .<sup>13</sup> On the other hand, around the equilibrium geometry of the strong complex OC-BH<sub>3</sub>, the three attractive interactions, ES, CT, and PL, are found to be of comparable magnitude and are all essential for binding of the complex.<sup>14</sup> This complex can be called an "electrostatic-charge-transfer polarization complex". In the even stronger borazane complexes,  $H_3N-BH_3$  and  $H_3N-BF_3$ , ES is found to be much larger than CT and PL and is the only attractive term required to keep the complex bound.14 These complexes are therefore "strong electrostatic complexes".

In the present paper, after the Introduction (section II), we present the results of ECDD analyses for several halogen complexes: H<sub>3</sub>N-F<sub>2</sub>, H<sub>3</sub>N-Cl<sub>2</sub>, H<sub>3</sub>N-ClF, CH<sub>3</sub>H<sub>2</sub>N-ClF (these all in section III), H<sub>2</sub>CO-F<sub>2</sub> (section IV), HF-ClF (section V), and  $(F_2)_2$  (section VI). The first four of these have been subjected to an MO study by Lucchase and Schaefer,<sup>18</sup> who found that a minimal basis set gave results which were very different from two larger basis sets: a double- $\zeta$  set and a double- $\zeta$  plus polarization set. The present ECDD analysis should clarify subtle differences in relative binding capabilities of donors such as H<sub>3</sub>N and CH<sub>3</sub>H<sub>2</sub>N and of acceptors such as ClF, Cl<sub>2</sub>, and F<sub>2</sub>. The dramatic contrast in the effect of alkyl substitution, i.e., the large effect in the proton affinity of ammonia and amines  $R_1R_2R_3N$ , and the almost total absence of such an effect in the binding energy of amine-BH3 complexes has been attributed to PL and EX; the increase in the PL stabilization and the increase in the EX repulsion upon successive alkylation cancel one another in the complex with BH<sub>3</sub>, whereas EX repulsion does not exist in the complex with  $H^+$ . thus leaving the PL effect uncancelled.<sup>14,15</sup> The ECDD analysis for the present complexes is also expected to shed light on the origin of alkyl substituent effects. The  $H_2CO-F_2$  complex has been picked as a model for well-known complexes between ketones and Br<sub>2</sub> and I<sub>2</sub>.<sup>2</sup>

The HF-ClF complex has recently been found by Janda, Klemperer, and Novick in the molecular beam microwave spectroscopy and its structure has been determined.<sup>19</sup> At the present time, the non-hydrogen bonded complex of the form HF-ClF is the only form which has been observed, while its hydrogen bonded counterpart FH-FCl has gone undetected. A comparison of the stable structures in both non-hydrogen bonded and hydrogen bonded complexes is a topic of the present study. The ECDD analysis also enables a direct comparison of the origin of bonding between two forms of the complex, serving as a guide for a unified theory of EDA complexes and hydrogen bonds. The fluorine dimer,  $(F_2)_2$ , has been chosen as a model of another halogen dimer,  $(Cl_2)_2$ , which has recently been found to be a polar molecule with a dipole moment about 0.2 D or greater.<sup>20</sup> (F<sub>2</sub>)<sub>2</sub> itself appears to be a polar molecule with a dipole moment on the order of 0.1 D.<sup>21</sup> A model of an "L" shaped or a "T" shaped dimer has been proposed for the geometry of (Cl<sub>2</sub>)<sub>2</sub>, based on the structure of the Cl<sub>2</sub> crystal and on the quadrupole–quadrupole interaction scheme.<sup>20</sup> We examine the geometry of the (F<sub>2</sub>)<sub>2</sub> complex, employing an estimate of the dispersion energy as well as  $\Delta E_{SCF}$ . The final section of the paper is a summarizing discussion (section VII) on the overall picture of the EDA interaction obtained in this series of papers.

#### **II. Methods and Geometries**

All the calculations of  $\Delta E_{SCF}$  have been carried out within the closed shell LCAO-SCF approximation with the 4-31G split valence-shell basis set with recommended exponents, contraction coefficients, and scale factors.<sup>22a</sup> The GAUSSIAN 70 program with our own ECDD analysis routines has been used.<sup>22b</sup> The 4-31G basis set is flexible enough to give a reasonable estimate of the interaction energy and its components. However, it does have a tendency to exaggerate the polarity of molecules, resulting in an overestimate of the interaction energy, particularly ES.9,11,23 When a delicate comparison of different stable geometries of a complex was required, as in the HF-ClF complex, the 4-31G\*\* basis set which includes one set of polarization functions on each atom (a p function with the exponent  $\alpha = 1.1$  for a hydrogen atom and a d function with  $\alpha = 0.8$  for other atoms)<sup>24</sup> was adopted, in addition to 4-31G. The IBMOLH program has been used for the evaluation of integrals involving d functions.<sup>25</sup> This basis set, to a great extent, alleviates the problem of exaggerated polarities experienced with the less flexible 4-31G set. The calculated and experimental dipole moments of the acceptors and donors are shown in Table I.

The geometries of the monomers were taken from experimental results, unless otherwise noted. F<sub>2</sub>, r(F-F) = 1.417 Å; CIF, r(CI-F) = 1.628 Å; Cl<sub>2</sub>, r(CI-CI) = 1.988 Å;<sup>26</sup> H<sub>3</sub>N, r(N-H) = 1.0124 Å and  $\angle HNH = 106.67^{\circ};^{27}$  CH<sub>3</sub>H<sub>2</sub>N, C<sub>s</sub>. staggered, r(C-N) = 1.451 Å,  $r(CH_s) = 1.109$  Å,  $r(CH_a) = 1.088$  Å,  $\angle CNH = 110.9^{\circ}$ ,  $\angle NCH_s = 111.7^{\circ}$ ,  $\angle NCH_a = 110.1^{\circ}$ ,  $\angle H_aCH_s = 108.1^{\circ}$ ,  $\angle H_aCH_a = 108.6^{\circ}$  (above from Me<sub>3</sub>N),<sup>28</sup> and r(N-H) = 1.0124 Å (from NH<sub>3</sub>) where H<sub>s</sub> is on a symmetry plane and two H<sub>a</sub>'s are not; H<sub>2</sub>CO, C<sub>2c</sub>, r(C-H) = 1.102 Å, r(C=O) = 1.210 Å,  $\angle HCH = 121.1^{\circ};^{27}$ HF, r(H-F) = 0.9171 Å.<sup>29</sup> They were assumed to be unchanged upon complex formation. Only a limited optimization of the geometry of complexes was carried out with respect to intermolecular distances and angles.

For  $(F_2)_2$  the dispersion energy DISP has been estimated by the second-order perturbation scheme, as was described previously.<sup>13</sup>

$$DISP = -4 \sum_{i}^{occ} \sum_{k}^{vac} \sum_{\mu}^{occ} \sum_{\nu}^{vac} \frac{|(i_{A}k_{A}|\mu_{B}\nu_{B})|^{2}}{E_{i\to k}^{A} + E_{\mu\to\nu}^{B} - E_{0}^{A} - E_{0}^{B}}$$
(3)

where  $\langle i_A k_A | \mu_B \nu_B \rangle$  is a two-electron integral over the SCF-MO's of isolated molecules. Terms in the denominators such as  $E_0^A$  and  $E_{\mu \to \nu}^B$  are the unperturbed energies of isolated molecules in the ground and singly excited states.

The ECDD analysis has been performed with the method of Kitaura and Morokuma.<sup>8</sup> The definitions of energy and charge distribution components and mechanics of calculation have been summarized in one of our recent papers<sup>14</sup> and will not be repeated here. When an analytic potential as a function

 
 Table I. Experimental and Calculated Dipole Moment of Monomers (in D)

	Exptl	Calcd 4-31G
NH <sub>3</sub>	1.468 <i>a</i>	2.30
CIF	$2.1 \pm 1.4 (Cl^{-}F^{+})^{b}$	1.58 (Cl+F-)
	0.884	
	$0.81 (Cl^+F^-)^d$	
H <sub>2</sub> O	1.85 <sup>e</sup>	2.60
НF	1.83 <sup>f</sup>	2.28
H <sub>2</sub> CO	2.338	3.00

<sup>a</sup> C. H. Townes and A. L. Schawlow, "Microwave Spectroscopy", McGraw-Hill, New York, N.Y., 1955. <sup>b</sup> J. J. Ewing, H. L. Tigelaar, and W. H. Flygare, J. Chem. Phys., **56**, 1957 (1972). <sup>c</sup> R. E. Davis and J. S. Muenter, *ibid.*, **57**, 2836 (1972). <sup>d</sup> Reference 19. <sup>e</sup> T. R. Dyke and J. S. Muenter, J. Chem. Phys., **59**, 3125 (1973). <sup>f</sup> J. S. Muenter and W. Klemperer, J. Chem. Phys., **52**, 6033 (1970). <sup>g</sup> K. Kondo and T. Oka, J. Phys. Soc. Jpn., **15**, 307 (1960).

of a geometric variable was necessary, a rational fraction was fit to the calculated data points.<sup>14</sup> In sections III–V,  $\Delta E$  is used to mean  $\Delta E_{SCF}$ .

### III. Ammonia and Amine-Halogen Complexes

(A) H<sub>3</sub>N-F<sub>2</sub>. First we examined the interaction energy components of the H<sub>3</sub>N-F<sub>2</sub> complex as a function of the intermolecular separation  $R = r(N-F_a)$  as one end F<sub>a</sub> of the fluorine molecule approaches N of NH<sub>3</sub> maintaining the overall C<sub>3v</sub> symmetry. The results are shown in Table II.



At the calculated equilibrium separation  $R_e = 3.00$  Å, the electrostatic energy, ES, and the charge transfer energy, CT, are the largest contributors to the stabilization, while the polarization energy, PL, makes a minor contribution. A large ES contribution is somewhat of a surprise for a complex of a nonpolar monomer molecule. It is recognized, however, that  $F_2$  has a permanent quadrupole (and higher multipoles) and that its interaction with a large dipole moment (and higher multipoles) of H<sub>3</sub>N can result in a substantial ES. Our ES, which is derived from the full electron distribution rather than multipole expansion, of course includes all the multipole interactions. CT consists of the  $H_3N \rightarrow F_2$  charge transfer, the  $H_3N \leftarrow F_2$  back donation, and their coupling.<sup>8</sup> Though we have not separated these terms, presumably the charge transfer from the highest occupied N lone pair (n) orbital of  $NH_3$  to the lowest vacant  $\sigma^*$  orbital of F<sub>2</sub> is the principal contribution to CT stabilization. This conjecture is supported by the components of the changes in the gross atomic population shown in Table III and by the plots of electron density changes in Figure 1. A charge transfer takes place from NH<sub>3</sub> to F<sub>2</sub> along the  $C_{3v}$  axis via  $\sigma$  orbitals. The PL effect causes a large (compared to other effects) shift of electron distribution in  $F_2$ , inducing a dipole  $F_a^{+\delta} - F_b^{-\delta}$ . The principal contribution to the PL energy, therefore, should come from the interaction of the permanent polarity of NH<sub>3</sub> with an induced polarity of F<sub>2</sub>. As is seen in Figure 1, a small additional polarity is  $-\delta' + \delta' N$ - $-\delta'+\delta'H_3$  is induced on H<sub>3</sub>N by a large induced polarity in F<sub>2</sub>. EX causes a small depletion of electron density from the interaction region as is seen in Figure 1.

In order to find out which components are necessary to keep a bound complex, we have plotted, as a function of R, the

**Table II.** Energy Decomposition Analysis for the Complex  $H_3N-F_2$  at Various Separations in kcal/mol ( $C_{3c}$  and Perpendicular Approaches)

		$C_{3\iota}$	(1)		Perpendicular (2)
R, Å	2.68	3.00 <i>ª</i>	3.08	3.48	3.00
$\Delta E$	-0.82	-1.05	-1.00	-0.59	0.53
ES	-1.67	-0.76	-0.65	-0.35	-0.07
EX	2.57	0.61	0.42	0.06	0.98
PL	-0.52	-0.28	-0.24	-0.12	-0.09
СТ	-1.30	-0.64	-0.54	-0.18	-0.30
MIX	0.11	0.03	0.02	0.00	0.01

<sup>a</sup> The equilibrium R determined from a parabolic fit. The energy and its components are actual calculated values.

truncated interaction  $\Delta E^{tr}$  in which one attractive component (ES, PL, or CT) is removed. The equilibrium intermolecular separations  $R_e^{tr}$  and the energies  $\Delta E_e^{tr}$  at  $R_e^{tr}$  for various truncated interaction curves are shown in Table IV. It is clear from Table IV that both ES and CT are necessary for a bound complex. This is a weak "ES-CT complex".

A deviation of the F<sub>2</sub> approach from the NH<sub>3</sub>  $C_{3v}$  axis decreases the stabilization of the complex.<sup>18</sup> In order to investigate the origin of this change, we examined an approach in which the F<sub>2</sub> molecular axis is perpendicular to the  $C_{3v}$  axes with one of the fluorine atoms, F<sub>a</sub>, on the  $C_{3v}$  axes. The results



at R = 3.00 Å are shown in the last column of Table II. A comparison with the  $C_{3v}$  approach at the same R indicates that all the components destabilize the complex upon deviation from  $C_{3v}$ , the most notable contribution being ES, followed by EX and CT. The ES destabilization can be understood as follows. If the electron distribution is spherical around the atom F<sub>a</sub>, the deviation should not change ES between NH3 and Fa. Actually an F atom has two  $p\pi$  electrons in each direction but only one  $p\sigma$  electron. Therefore the F<sub>2</sub> electron distribution is more dense (negative) to the direction perpendicular to the bond axis than along the axis. Therefore the electron rich N atom should prefer the axial approach. This contention is supported by calculating for F<sub>2</sub> the electrostatic potential  $\phi(r)$ , i.e., the electrostatic interaction energy when a unit positive charge (e.g., proton) is at r. The 4-31G wave function gives  $\phi(r) =$ -428.6 kcal/mol at 3 Å from the closer F atom along the F<sub>2</sub> bond axis, and  $\phi(r) = -443.7$  kcal/mol at 3 Å from an F atom in the direction perpendicular to the bond axis. A unit positive charge is stabilized more in the perpendicular approach, and this approach is less favored for the electron rich N atom of  $NH_{3}$ .

 $NH_3$  and  $F_2$  can interact through hydrogen bonding to form a complex  $H_2NH-F_2$ . We have not examined such an approach for any  $H_3N$ -halogen complexes. A comparison of hydrogen bonded and non-hydrogen bonded complexes will be made for FCl-FH in section V.

(B)  $H_3N$ -ClF. This system has been chosen for comparison with  $H_3N$ - $F_2$  and  $H_3N$ - $Cl_2$ ; ClF has a permanent dipole whereas  $F_2$  and  $Cl_2$  are, of course, nonpolar. We first examined the  $C_{3v}$  complex, in which the Cl end of ClF approaches the N of the NH<sub>3</sub>. This orientation was found to be the most favored approach.<sup>18</sup>

**Table III.** Gross Atomic Electron Population of Isolated Molecules and Its Component Changes for the Complex  $H_3N-F_2$  ( $C_{3c}$  Approach, R = 3.00 Å)

	NI	NH <sub>3</sub>		$F_2$	
	Н	N	Fa	F <sub>b</sub>	$[H_3N \underset{(-)}{\overset{(+)}{\longleftrightarrow}} F_aF_b{}^a]$
Isolated molecule	0.7078	7.8945	9.0000	9.0000	
Total change <sup>b</sup>	-0.0027	0.0045	-0.0337	0.0373	0.0035
EX <sup>b</sup>	0.0	0.0	-0.0003	0.0003	
PL <sup>b</sup>	-0.0021	0.0062	-0.0342	0.0342	
CT <sup>b</sup>	0.0	-0.0037	0.0030	0.0007	0.0036
MIX <sup>b</sup>	-0.0007	0.0021	-0.0023	0.0022	-0.0001

<sup>*a*</sup> A positive value indicates a net charge transfer from NH<sub>3</sub> to  $F_2$  and negative from  $F_2$  to NH<sub>3</sub>. <sup>*b*</sup> Positive and negative values indicate an increase and a decrease, respectively, of electron population upon complex formation.

**Table IV.** Truncated Interaction Energy  $\Delta E^{tr}$  and Equilibrium Separation  $R_e^{tr}$  for  $H_3N-F_2$  ( $C_{3c}$  Approach)

$\Delta E^{tr}$	$R_{\rm e}^{\rm tr}$ , Å	$\Delta E_{e}^{Ir}$ , kcal/mol
$\Delta E$	3.00	-1.05
$\Delta E-ES$	3.22	-0.39
$\Delta E-PL$	3.02	-0.77
$\Delta E-CT$	3.24	-0.50



Table V shows the results as functions of R = r(N-Cl). At the calculated equilibrium  $R_{\rm e}$ , the complex is highly electrostatic in nature, with a substantial additional contribution from CT. The equilibrium separation  $R_e^{tr}$  from truncated potential energy curves, shown in Table VI, suggests that the removal of ES would make the complex only weakly bound and that the lack of CT would also have a substantial influence on the binding. Though the sign of the experimental dipole moment of Cl appears to be a subject of controversy (Table I), a comparison of these with accurate ab initio calculations by Green (1.099 D Cl<sup>+</sup>F<sup>-</sup> for the Hartree-Fock and 0.839 D Cl<sup>+</sup>F<sup>-</sup> for the CI calculation)<sup>30</sup> suggests that the present 4-31G dipole is of the correct sign but the magnitude is overestimated. Even if such an overestimation is taken into account, the complex can still be characterized as a "ES-CT or ES complex" of intermediate strength.

A comparison of this complex with another "ES-CT complex",  $H_3N-F_2$ , which is very weak, is interesting. The chlorine atom has a bulkier electron distribution, i.e., a larger van der Waals radius, than the fluorine atom. This is reflected in different energy components in the two complexes at about the same separation R, e.g., 3.00 and 3.08 Å for  $H_3N-F_2$  in Table II and 3.05 Å for  $H_3N-ClF$  in Table V. Because of a bulkier electron cloud, the ClF complex has a larger EX repulsion and also larger CT and PL attractions than the  $F_2$  complex. At such a large distance, however, ES is the predominant term; the  $H_3N-ClF$  complex is an ES complex. The strong ES attraction pulls the molecules closer together, resulting in a much smaller  $R_e$ . At a smaller R, the relative importance of CT increases rather drastically, making this complex an "ES-CT complex" of intermediate strength.

The results of electron population decomposition and the plots of electron density components near the calculated  $R_e$  are shown in Table VII and Figure 2, respectively. Since  $R_e$  is smaller, an order of magnitude larger charge transfer takes place in H<sub>3</sub>N-ClF than in H<sub>3</sub>N-F<sub>2</sub> (Table III and Figure 1). CT is from NH<sub>3</sub> to ClF along the  $C_{3v}$  axis through the  $\sigma$  or-

**Table V.** Energy Decomposition Analysis for the Complex  $H_3N$ -CIF at Various Separations in kcal/mol ( $C_{3c}$  and Perpendicular Approaches)

		$C_{3t}$ (3)		Perpendi	cular (4)
R, Å	2.25	2.65	2.717 <i>ª</i>	3.05	2.717
$\Delta E$	-4.68	-8.16	-8.23	-6.43	8.50
ES	-36.86	-12.96	-11.18	-6.23	-5.32
EX	47.53	10.02	7.41	2.02	15.32
PL	-3.71	-1.23	-1.05	-0.55	-0.38
СТ	-12.62	-4.22	-3.59	-1.77	-1.26
MIX	0.98	0.24	0.19	0.10	0.13

<sup> $\alpha$ </sup> The equilibrium R and energy components determined for a parabolic fit.

**Table VI.** Truncated Interaction Energy  $\Delta E^{tr}$  and Equilibrium Separation  $R^{tr}$  for H<sub>3</sub>N-ClF ( $C_{3c}$  Approach)

$\Delta E^{\mathrm{tr}}$	$R_{\rm e}^{\rm tr}$ , Å	$\Delta E_{\rm c}^{\rm tr}$ , kcal/mol
$\Delta E$	2.72	-8.23
$\Delta E-ES$	2.94	-1.06
$\Delta E-PL$	2.79	-7.36
$\Delta E-CT$	2.88	-5.72

bitals. This can be seen clearly in  $\rho_{CT}$  of Figure 2 with the transferred charge accumulating in the intermolecular region. However, EX and PL of CIF both shift the electron cloud away from the interaction region; the overall  $\Delta \rho$  shows a depletion of electron distribution between N and Cl. A large polarization of NH<sub>3</sub> as well as CIF is observed in  $\rho_{PL}$ .

We also examined the approach in which the ClF axis staggered with respect to the NH<sub>3</sub> is perpendicular to the  $C_{3v}$ axis, with the Cl atom on the  $C_{3v}$  axis (Table V). This approach



is strongly repulsive at R = r(N-Cl) = 2.717 Å. When compared with the  $C_{3v}$  approach, this unstability is mainly due to an increase in the EX repulsion and a decrease in the ES stabilization. The misalignment of permanent dipoles qualitatively explains the decrease in ES. Despite a polarity  $Cl^+F^-$ , the electron density on the chlorine atom is more dense along the  $\pi$  axis (because  $\pi$  orbitals are saturated) than the  $\sigma$  axis, as was discussed for the F<sub>2</sub> complex. As a result, the EX repulsion is probably larger in the perpendicular approach than the  $C_{3v}$ approach.

	NI	NH <sub>3</sub>		CIF		
	Н	N	Cl	F	$H_3N \stackrel{(+)}{\underset{(-)}{\leftarrow}} ClF^a$	
Isolated molecule	0.7078	7.8945	16.6050	9,3950		
Total change <sup>b</sup>	-0.0234	0.0316	-0.0328	0.0713	0.0385	
EX <sup>b</sup>	0.0003	-0.0010	-0.0055	0.0055	0.00000	
PL <sup>b</sup>	-0.0201	0.0604	-0.0470	0.0470		
CT <sup>b</sup>	0.0	-0.0350	0.0303	0.0047	0.0349	
MIX <sup><i>h</i></sup>	-0.0036	0.0072	-0.0106	0.0141	0.0036	

**Table VII.** Gross Atomic Electron Population of Isolated Molecules and Its Component Changes for the Complex  $H_3N-ClF(C_{3v}$ Approach, R = 2.65 Å)

<sup>*a*</sup> A positive value indicates a net charge transfer from NH<sub>3</sub> to CIF and negative from CIF to NH<sub>3</sub> <sup>*b*</sup> Positive and negative values indicate an increase and a decrease, respectively, of electron population upon complex formation.



Figure 1. Component electron density maps for the complex  $H_3N-F_2$  at r(N-F) = 3.00 Å in the  $C_{3c}$  approach. Full lines indicate density increases and dotted lines indicate decreases. Contours are successively  $\pm 1$ ,  $\pm 3$ ,  $\pm 5$ ,  $\pm 7 \times 10^{-4}$  (Bohr<sup>-3</sup>). The coordinates are in Å, relative to the inner F atom, and plotting is made for the FFNH plane.

Table VIII shows the results of energy decomposition as functions of R = r(N-F) for a  $C_{3v}$  complex in which the F end of ClF approaches N of NH<sub>3</sub>. The complex was found to be unbound. This is, in principle, due to the repulsive ES interaction, whereas PL, EX, and CT components are of compa-



**Figure 2.** Component electron density map for the complex  $H_3N$ -ClF at r(N-F) = 2.65 Å in the  $C_{3c}$  approach. The coordinates are relative to Cl and plotting is made for the FCINH plane. See Figure 1 for other details.



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**Table VIII.** Energy Decomposition Analysis for the Complex  $H_3N$ -FCl (4) at Various Separations in kcal/mol ( $C_{3c}$  Approach)

	<i>R</i> , Å		
	2.65	3.05	3.45
$\Delta E$	4.55	2.31	1.59
ES	2.84	2.46	1.82
EX	3.30	0.58	0.08
PL	-0.58	-0.28	-0.14
СТ	-1.11	-0.47	-0.17
MIX	0.11	0.02	0.00

rable magnitude with those in the  $H_3N-F_2$  complex (Table II).

(C) CH<sub>3</sub>H<sub>2</sub>N-ClF and N-Methyl Substituent Effect. As was discussed in section I, the N-methyl substituent effect on the energy of the H<sub>3</sub>N-BH<sub>3</sub> complex formation is in marked contrast with the analogous effect on the proton affinity of NH<sub>3</sub>. Lucchese and Schaefer compared the difference in the complexing ability of NH<sub>3</sub> and N(CH<sub>3</sub>)<sub>3</sub> with F<sub>2</sub>, ClF, or Cl<sub>2</sub> employing the minimal STO-3G basis set.<sup>18</sup> Since this set predicts the polarity Cl<sup>-</sup>F<sup>+</sup> which is opposite to that attained from both better theoretical calculations and the recent experiment results discussed in section IIB, and since this set also has a tendency to overestimate the CT contribution, the interpretations obtained from their calculation are questionable.

The second column of Table IX shows the energy components for the  $H_3N-ClF$  complex at the calculated equilibrium  $(C_{3v})$  geometry and their differences in parentheses between  $CH_3H_2N-ClF$ , **6**, and  $H_3N-ClF$  at the same geometry. The



*N*-methyl substitution lowers the stabilization energy of the complex by a small amount. This is consistent with previous STO-3G calculations but is in the opposite direction and of much smaller magnitude than the change in  $\Delta H$  observed in solution for amine-iodine complexes.<sup>31</sup> The disagreement could be either due to the deficiency of the present theory or due to the solvent effect. One may note that molecular orbital calculations for the methyl substituent effect.<sup>15</sup> on the proton affinity of amines agree well with the gas phase experiment which is substantially different from the experiment in solution.<sup>32</sup> The proton affinity of amines in solution is known to change in the order:

$$NH_3 < RNH_2 \cong R_2NH > R_3N$$

whereas in the gas phase the proton affinity monotonically increases in the order:  $^{32}$ 

$$NH_3 < RNH_2 < R_2NH < R_3N$$

The energy decomposition indicates that the decrease in the stabilization of the  $H_3N$ -ClF complex upon methylation is principally due to an increase in the EX repulsion, supplemented by a decrease in the ES stabilization. These effects are partially negated by an increase in the CT stabilization. Table IX also summarizes the calculated *N*-methyl substituent effects for the  $H_3N$ -BH<sub>3</sub>, 7, and the  $H_3N$ -H<sup>+</sup>, 8, complex. These two complexes show an additional stabilization upon methylation, in contrast to the  $H_3N$ -ClF case. The ratio of the

**Table IX.** A Comparison of Interaction Energy Components andN-Methyl Substituent Effects between Various Complexes atEquilibrium Geometry in kcal/mol

	$H_3N-ClF(6)$	$H_3N-BH_3(7)^a$	$H_3N-H^+(8)^b$
R, Å	2.717	1.705	1.02
$\Delta E$	-8.23	-44.7	-221.9
ES	-11.18	-92.9	-99.8
EX	7.41	86.9	0.0
PL	(0.53) -1.05	(4.4) -17.2	-27.4
СТ	(0.02) -3.59	(-5.0) -27.1	(-12.8) -88.3
MIX	(-0.57) 0.19 (-0.01)	(-1.4) 5.6 (2.4)	(-3.4) -6.5 (4.4)

"Reference 14. <sup>*b*</sup> Reference 15. <sup>*c*</sup> The numbers in parentheses are the difference between the  $CH_3H_2N$  complex and the  $H_3N$  complex. A negative number indicates that the  $CH_3H_2N$  complex is more stable, and vice versa.

difference in the stabilization energy between the CH<sub>3</sub>H<sub>2</sub>N and the H<sub>3</sub>N complex versus the stabilization energy of the H<sub>3</sub>N complex should provide a relative guide for the magnitude of the methyl substituent effect. The ratio is 4, 2, and 4% for the complex with ClF, BH<sub>3</sub>, and H<sup>+</sup>, respectively. The substituent effect for H<sub>3</sub>N-BH<sub>3</sub> is indeed found experimentally to be very small in the gas phase.33 An increase in the CT stabilization is common to all three complexes and can probably be attributed to the lowering of the donor's experimental ionization potential (234.1 kcal/mol for NH<sub>3</sub> to 206.8 kcal/ mol for  $H_3CNH_2$ )<sup>34</sup> or, correspondingly, the increase in the donor's calculated highest occupied MO energy (-252.5 for)NH<sub>3</sub> to -233.0 kcal/mol for H<sub>3</sub>CNH<sub>2</sub> in the present calculation). The decrease in the ES stabilization is probably due to a small increase in the electron population on the N atom (7.89 for NH<sub>3</sub> to 7.81 for  $H_3CNH_2$  in the present calculation). The  $H_3NH^+$  case is in accord with the present result, but the  $H_3N-BH_3$  complex shows an opposite trend. This anomaly is due to the fact, presumably, that the H<sub>3</sub> group of BH<sub>3</sub> can also influence the change in ES. The increase in EX is noted both for this complex and  $H_3N-BH_3$  while it does not exist in the  $H_3N-H^+$  complex because the proton does not have an electron. The increase in EX is presumably due to the interaction of the CH<sub>3</sub> group with the acceptor electrons. It is extremely interesting to note among these three complexes differences in which term is the primary contribution to the total stabilization, as well as differences in dominant terms for the methyl substituent effect. The results are summarized as follows:

(a)  $H_3N$ -ClF: stabilization, ES supplemented by CT; Me substitution, destabilization (EX, cancelled almost evenly by CT, supplemented by ES; components of order of 0.5 kcal/mol).

(b)  $H_3N-BH_3$ : stabilization, ES; Me substitution, small stabilization (PL, cancelled mostly by EX; components of order of 5 kcal/mol).

(c)  $H_3N-H^+$ : stabilization, ES and CT; Me substitution, stabilization (PL; components of order of 10 kcal/mol).

(D) H<sub>3</sub>N-Cl<sub>2</sub>. The H<sub>3</sub>N-Cl<sub>2</sub> complex will provide a reasonable form of comparison with H<sub>3</sub>N-F<sub>2</sub> in regard to the size of electron clouds of the acceptor molecule as well as with H<sub>3</sub>N-ClF in regard to the polarity of the acceptor. A calculation was carried out for H<sub>3</sub>N-Cl<sub>2</sub> in a  $C_{3c}$  (collinear NCl<sub>a</sub>Cl<sub>b</sub>) geometry at  $R = r(N-Cl_a) = 2.93$  Å, the optimal geometry by Lucchese and Schaefer in a double- $\zeta$  basis set.<sup>18</sup> The results are  $\Delta E = -2.89$ , ES = -3.98, EX = 3.94, PL =

**Table X.** Energy Decomposition Analysis for the Complex  $H_2CO-F_2$  (9) at the Various Separations in kcal/mol<sup>*a*</sup>

		R,Å	
	2.60	2.90	3.20
$\Delta E$	-0.44	-0.68	-0.46
ES	-0.86	-0.42	-0.26
EX	1.43	0.32	0.06
PL	-0.17	-0.10	-0.06
CT	-0.92	-0.50	-0.22
MIX	0.08	0.02	0.00

" A parabolic fit of these three points gives  $R_e = 2.907$  Å.

-0.81, CT = -2.30, and MIX = 0.26 kcal/mol. In comparison with the results in Table II for  $H_3N-F_2$ , one finds that, though  $R_e$  is similar, the complex Cl<sub>2</sub> is stronger with all the components several times larger than their counterparts in the F<sub>2</sub> complex. The most notable increases are observed for EX (seven times with respect to the  $F_2$  complex at 3.00 Å) and ES (five times). Since the Cl<sub>2</sub> valence electron cloud is more widely spread out, the electron donor molecule can penetrate deeper in the cloud resulting in a larger ES, CT, as well as PL before it feels the very steep wall of EX repulsion. A comparison with Table V shows that the increase in the stabilization in the  $H_3N-ClF$  complex relative to the  $H_3N-Cl_2$  complex at the same distance (2.93 Å) is principally due to a twofold increase in ES, partially negated by a small increase in the EX repulsion. Both changes may be attributed to an increase in the electron density on the chlorine atom.

Summarizing  $H_3N$ -halogen complexes, one may call  $H_3N$ -ClF "an ES complex" of an intermediate strength since the contribution of the next largest term CT is only 30% of ES.  $H_3N$ -Cl<sub>2</sub> and  $H_3N$ -F<sub>2</sub> are both "weak ES-CT complexes" with the CT contribution more than a half of ES.

#### IV. The H<sub>2</sub>CO-F<sub>2</sub> Complex

As a model for another series of weak halogen complexes we studied the complex between  $H_2CO$  and  $F_2$ . Concordant with the geometry of the acetone-Br<sub>2</sub> complex in the crystal,<sup>35</sup>  $F_2$  was assumed to approach the O atom of  $H_2CO$  collinearly within the  $H_2CO$  molecular plane with a COF angle of 120° (9). Table X summarizes the results of an energy decomposi-



tion as a function of  $R = r(O-F_a)$ . The complex is one of the most weakly bound systems which we studied in the present paper. A comparison with the  $H_3N-F_2$  complex (Table II) is of particular interest, since both are weak complexes. The equilibrium intermolecular separation R = r(O-F) = 2.91 Å for H<sub>2</sub>CO-F<sub>2</sub> is smaller than R = r(N-F) = 3.00 Å for  $H_3N-F_2$ , even though the former is a weaker complex. This is due to the smaller size of electron cloud on O than on N and consequently a smaller EX repulsion for the former complex at the same R. This same factor is also responsible for a smaller CT attraction for  $H_2CO-F_2$ . The net charge on N of  $NH_3$  is -0.89 (Table III) and is larger than that on O of H<sub>2</sub>CO (-0.48in Table XI). Though the dipole moment of NH<sub>3</sub> is smaller than that of  $H_2CO$  (Table I), one expects that  $NH_3$  will give rise to a larger ES interaction than H<sub>2</sub>CO, because the nearest charge-charge interaction is more important than the dipole-dipole interaction in determining the global ES. This is indeed what is found as is evident from a comparison of Tables

II and X at the same distance. Overall, each component of the  $H_2CO$  complex is about a half or two-thirds as large as that of the NH<sub>3</sub> complex. Truncated potential energy  $\Delta E^{tr}$  plots indicate that both ES and CT make significant contributions to the binding. Therefore, this complex as well as  $H_3N-F_2$  may be called a weak "ES-CT complex". The population analysis in Table XI for  $H_2CO-F_2$  shows a smaller charge migration for each component than for  $H_3N-F_2$  at a somewhat larger distance (Table III). The polarization of  $H_2CO$  by  $F_2$  causes the migration of charge from O to the CH<sub>2</sub> group. The separate  $\pi$  and  $\sigma$  population changes by CT indicate that the contribution of  $\pi$  CT is negligible. This is primarily because  $R_c$  is so large (2.91 Å) that the  $\pi$ -type overlap between  $\pi$  orbitals is not significant.

# V. ClF-HF and FCl-FH. Hydrogen Bonded and Antihydrogen Bonded Complexes

As was discussed briefly in section I, a very recent study using microwave and radio frequency spectroscopy with a nozzle molecular beam electric resonance technique has determined the structure and dipole moment of a weakly bound non- or anti-hydrogen bonded complex FCl-FH.<sup>19</sup> The structure **10** has the following parameters: r(F-Cl) = 2.7744

$$F_{a}$$
  
 $\gamma$   $Cl - - F_{b}$   $H$ 

Å,  $\angle ClF_bH = 115 \pm 5^\circ$ ,  $\gamma = \pi - \angle F_bClF_a = 4.94^\circ$  (if planar), and the unknown azimuthal angle is set equal to 0. Observed dipole moments of the complex for three isotopic combinations have been used to deduce that the sign of the dipole moment of ClF is Cl<sup>+</sup>F<sup>-</sup>. So far the hydrogen bonded counterpart FCl-HF has gone undetected. This system provides a unique opportunity to compare ECDD analyses of hydrogen bonded and non-hydrogen bonded structures within a single complex.

(A) Geometry Optimization. It is of interest to determine whether calculations of the present level will yield geometrical results concordant with the experiment. A geometry optimization is carried out with the restriction that the CIF molecule and the F<sub>b</sub> atom of HF are collinear, a restriction rationalized by the fact that the experimental value of  $\gamma$  is small. A series of calculations as functions of  $R = r(F_b-Cl)$  and  $\angle ClF_bH$  in Table XII give the optimized geometry as  $R = 2.73_7$  Å  $(\pm 0.027 \text{ Å}, \pm 0.08 \text{ Å})$  and  $\angle C1FH = 141^{\circ} (\pm 6^{\circ}, \pm 15^{\circ})$ . The error bounds are given arbitrarily for the energy difference of 0.006 and 0.06 kcal/mol, respectively, to illustrate roughly the flatness of the curve. In order to examine the effect of the non-linearity of F<sub>b</sub>, Cl, and F<sub>a</sub>, three additional calculations with  $\gamma = \pi - \angle F_b ClF_a = 10^\circ$  are carried out, as are shown in the last three rows of Table XII. The collinear interaction is favored, but for the same error bounds as above,  $\gamma = 0$  ( $\pm 2^{\circ}$ ,  $\pm$ 7°) for the eclipsed conformation, implying a small deviation is indeed possible if a more extensive search is made. The calculated geometry is in reasonable agreement with the experiment. Past experiences for (H<sub>2</sub>O)<sub>2</sub> and (HF)<sub>2</sub> suggest that the ClF<sub>b</sub>H angle is a quantity rather sensitive to the basis set and hard to predict accurately.1b,6b The inversion barrier for the FH proton is calculated to be only about 0.14 kcal/mol. The absolute value of this number is not reliable, since it depends strongly on the optimized ∠ClFH angle 141° which is in poor agreement with experiment  $115 \pm 5^{\circ}$ . However, one may say qualitatively that it is smaller than the corresponding barrier in (HF)2, where the 4-31G value is 0.35 kcal/mol with 2HFH =  $135^{\circ}$  vs. experimental  $119 \pm 5^{\circ}$ .

After a reasonable geometry of the anti-hydrogen bonded complex has been obtained, we turned our attention to the hydrogen bonded complex, **11**. A limited geometry optimiza-

Table XI. Gross Atomic Electron Population of Isolated Molecules and Its Component Charges for the Complex H<sub>2</sub>CO-F<sub>2</sub> (R = 2.90 Å<sup>a</sup>)

		H <sub>2</sub> CO			F <sub>2</sub>		
	Ha	H <sub>b</sub>	С	0	Fa	F <sub>b</sub> H	$_{2}CO \stackrel{(+)}{\underset{(-)}{\longleftrightarrow}} F_{a}F_{b}$
Isolated molecules	0.8447	0.8447	3.8267	8.4839	0.0	0.0	
Total change	-0.0017	-0.0017	-0.0015	0.0035	-0.0200	0.0214	0.0014
EX	0.0	0.0	0.0	0.0	-0.0001	0.0001	
PL	-0.0013	-0.0014	-0.0013	0.0038	-0.0200	0.0199	
СТ	0.0001	-0.0001	0.0001	0.0015	0.0014	0.0	0.0015
MIX	0.0005	-0.0002	-0.0003	0.0012	-0.0013	0.0013	-0.0001

<sup>a</sup> For sign conventions, see Table III.

Table XII. Geometry Optimization for the FCI-FH Complex 10

r(Cl-F <sub>b</sub> ), Å	∠ClF <sub>b</sub> H, deg	Total energy <sup>a</sup>
2.708	115	-0.101 667
2.758	115	-0.101 672
2.808	115	-0.101 615
2.858	115	-0.101 512
2.7369	115	-0.101 678
2.7369	135	-0.102 050
2.7369	155	-0.101 965
2.7369	180	-0.101 833
2.7369	141.27	-0.102 050
2.7369	141.27 (up 10) <sup>b</sup>	-0.101 841
2.7369	141.27 (down 10) <sup>b</sup>	-0.101 571
2.7369	141.27 (back 10) <sup>b</sup>	-0.101 714

<sup>a</sup> The entry -0.101 667, for instance, means the total energy -658.101 667 hartrees. <sup>b</sup> Structures with nonlinear  $F_aClF_b$ . In all cases  $\gamma = \pi - \angle F_bClF_a = 10^\circ$ . Azimuthal angles are 0° (eclipsed  $F_aClF_bH$ ) for "up", 180° (staggered) for "down", and 90° (the  $F_aClF_b$  plane perpendicular to the  $ClF_bH$  plane) for "back", respectively.

tion was carried out. Since the linear hydrogen bond is usually preferred,  $F_a$ , H, and  $F_b$  were assumed to be collinear. A series of calculations as functions of  $R = r(F_a-H)$  and  $\angle HF_aCl$ , as shown in Table XIII, yields the following prediction for the equilibrium hydrogen bonded geometry with the 4-31G set.  $r(F_a-H) = 1.86_4 \text{ Å}, \angle ClF_aH = 143^\circ, \Delta E = -4.7 \text{ kcal/mol}.$ Since  $r(F_{b}-H) = 0.917$  Å was assumed, this gives  $r(F_{a}-F_{b})$ = 2.78 Å. The barrier for inversion of the Cl atom is only 0.16 kcal/mol. As was mentioned above the  $ClF_aH$  angle and the inversion barrier are quantities sensitive to the basis set and full geometry optimization and hence are difficult to accurately evaluate. Nevertheless one might guess that the hydrogen bonded complex will be extremely floppy. The calculated geometry of this complex may be compared with that of (HF)<sub>2</sub>. Experimentally, r(F-F) = 2.79 Å,  $\angle HFH = 119 \pm 5^{\circ}$ , <sup>36</sup> and theoretically optimized with the present basis set in the same fashion as in this section,  $r(F-F) = 2.71 \text{ Å}, \angle HFH = 135^\circ, \Delta E$ = -7.6 kcal/mol, and barrier for inversion = 0.35 kcal/mol. In a qualitative comparison with  $(HF)_2$ , the ClF-HF complex is a weaker complex with a smaller  $|\Delta E|$  and a larger r(F-F)and has a smaller barrier for inversion of the external atom, with a less acutely bent geometry. Taking into account the error of the 4-31G results, we might make the following corrected predictions of the ClF-HF geometry:  $r(F_a-F_b) \sim 2.86$  $\dot{A}$ ,  $\angle ClF_aH = 130^\circ$ .

Though a definite determination has not been made, it ap-

 Table XIII. Geometry Optimization for the CIF-HF Complex 11

<i>r</i> (F <sub>a</sub> −H), Å	∠ClF <sub>a</sub> H, deg	Total energy <sup>a</sup>
1.867	180	-0.103 913
1.917	180	-0.103 866
1.967	180	-0.103 757
1.8546	180	-0.103 911
1.8546	155.93	-0.104 069
1.8546	150	-0.104 124
1.8546	140	-0.104 160
1.8546	130	-0.104 034
1.8639	142.81	-0.104 165

<sup>*a*</sup> The entry is the total energy + 658 hartrees.

 Table XIV. Interaction Energy and Its Components for FCI-FH

 and CIF-HF at the 4-31G Optimized Geometries (kcal/mol)

	4-310	}	4-31G**		
	Anti-H bonding	H bonding	Anti-H bonding	H bonding	
$\Delta E$	-3.35	-4.68	-3.23	-2.54	
ES	-3.62	-4.81	-2.96	-2.70	
EX	1.82	2.92	1.72	3.00	
PL	-0.22	-0.73	-0.24	-0.77	
CT	-1.41	-2.07	-1.87	-2.26	
MIX	0.08	0.02	0.12	0.19	

pears that both hydrogen bonded and anti-hydrogen bonded complexes are local minima on the potential energy surface.

(B) Polarized Basis Set. At the present level of calculation, the hydrogen bonded form seems to be about 1.3 kcal/mol more stable than the anti-hydrogen bonded form. However, the difference is rather small yielding this somewhat inconclusive result. Since the 4-31G set exaggerates the ES contribution, the relative energy of the two forms may be dependent on the choice of basis set. In order to examine this possibility, calculations were carried out with a 4-31G\*\* basis set at the 4-31 optimized geometries of both forms. This set has a p function on the hydrogen atom and a d function on the other atoms to facilitate the angular polarization of atomic orbitals.<sup>24</sup> The results of the calculations are shown in Table XIV. The relative stability of the two forms has reversed! In the 4-31G\*\* basis set, the anti-hydrogen bonded complex is found to be about 0.7 kcal/mol more stable than the hydrogen bonded complex. Still, the energy difference between the two forms is not large enough to be conclusive. Slight changes caused by the geometry reoptimization, a larger basis set, or the contribution of the dispersion energy and other correlation energy terms may, once again, tip the balance. If the two forms are indeed of nearly equal stability, there is a chance of finding

**Table XV.** Energy Components for Nonlinear FCI-FH around Calculated Equilibrium<sup>a</sup>

		Configuration				
	Linear	Up	Down	Back		
Azimuthal angle, deg		0	180	90		
$\Delta E$	-3.35	-3.22	-3.05	-3.14		
ES	÷3.62	-3.65	-3.42	-3.54		
EX	1.82	1.94	1.90	1.92		
PL	-0.22	-0.23	-0.20	-0.21		
СТ	-1.41	-1.35	-1.41	-1.38		
MIX	0.08	0.07	0.08	0.07		

"  $r(Cl-F_b) = 2.7369 \text{ Å}, \angle ClF_bH = 141.27^\circ, \gamma = \pi - \angle F_bClF_a = 10^\circ$ , except for linear configuration for which  $\gamma = 0$ . See text for description of configuration.

both or either one of them depending on the experimental condition. The present experimental situation that only the anti-hydrogen bonded species has been found<sup>19</sup> could mean either that this is much more stable than the other complex or that the nozzle beam condition selectively formed this complex.

Table XIV indicates that the difference between 4-31G and 4-31G\*\* results is principally due to the difference in ES, compensated slightly by CT. The decrease in ES attraction upon going from 4-31G to 4-31G\*\* is more pronounced for the hydrogen bonded complex (+2.1 kcal/mol) than for the anti-hydrogen bonded complex (+0.7 kcal/mol). Since the 4-31G\*\* basis set partially corrects the 4-31G's overestimate of ES, the 4-31G\*\* results are more likely to be correct.

(C) Energy and Charge Distribution in Decomposition Analyses. The effects of nonlinearity on the anti-hydrogen bonded complex were examined. Table XV shows energy decomposition results for the complex around  $r(Cl-F_b) = 2.7369$ Å and  $\angle ClF_bH = 141.27^\circ$ , the calculated equilibrium geometry. In all cases,  $\gamma = \pi - \angle F_b ClF_a = 10^\circ$ , and the azimuthal angle was taken to be 0° (eclipsed  $F_aClF_bH$ ) for "up", 180° (staggered) for "down", and 90° (FaClFb plane perpendicular to the ClF<sub>b</sub>H plane) for "back" configuration, respectively. The unstability of "down" and "back" configurations is principally due to a decrease in ES stabilization and an increase in EX repulsion. The "up" configuration is unfavored due to an increase in EX as well as a substantial loss in CT. Any deviation of  $F_a$  from the linearity will increase the overlap of electron clouds, leading to an increase in EX. The change in ES can be understood in terms of the polarity:  $F^{-\delta}Cl^{+\delta}$  and  $F^{-\delta'}H^{+\delta'}$ . The loss of CT in the "up" configuration can be attributed to a loss of overlap between the  $\pi$  and  $\sigma$  electron cloud of the donor and the acceptor's  $\sigma^*$  orbital, which is concentrated along the FaCl axis.

We have also performed energy decomposition analysis for both FCl-FH and ClF-HF complexes at the 4-31G level as

a function of the intermolecular separation. For FCI-FH a geometry with a collinear  $F_bClF_a$  and  $\angle ClF_bH = 115^\circ$ , which is similar to the experiment, was used. For ClF-HF a collinear  $(C_{\infty v})$  geometry was assumed. Table XVI shows the results. From Tables XVI and XIV, one finds that the anti-hydrogen bonded complex near the equilibrium is principally stabilized by ES, with a substantial supplement of CT. For the hydrogen bonded complex at the equilibrium R the stabilization is almost equally shared by ES and CT in the 4-31G\*\* basis set. Employing the 4-31G basis set the CT contribution is of the equally shared by ES and CT in the 4-31G\*\* basis set. Employing the 4-31G basis set the CT contribution is of the same magnitude as with the 4-31G\*\* set, while the ES contribution is still larger and appears to be overestimated. In light of this evidence one may say that the hydrogen bonded complex is a weak ES-CT complex, whereas the anti-hydrogen bonded complex is a weak ES or ES-CT complex. The component which displays the largest difference between the two forms of the complex is EX. For a comparable Cl-F and F-F distance, the HF proton in the hydrogen bonded complex is more deeply buried in the electron cloud than any atom of the antihydrogen bonded complex, presumably causing a large EX. PL contribution is of secondary importance in either complex but is larger in the hydrogen bonded complex, presumably again because the proton within a short distance exerts the largest influence on the electron clouds of the partner.

The electron density distribution decomposition provides an alternative and visual insight to the origin of bonding. Figures 3 and 4 are component electron density maps for FCI-FH and CIF-HF, respectively. Table XVII shows the corresponding component electron population for both complexes. The decomposition analysis reveals all the characteristics familiar with other hydrogen bonded and non-hydrogen bonded complexes studied by the authors (section III and ref 10 and 14), with some exceptions. EX removes the electron cloud from the interaction region, but its effect is rather small. CIF-HF experiences a larger EX electron shift than FCI-FH, which is reflected in EX repulsion in Table XIV. PL is the largest contributor to the electron redistribution, though its contribution to energy is small. PL gives rise to a polarity  $Cl^{-\delta+\delta}F$ --- $H^{-\delta+\delta}F$  in ClF-HF and  $F^{+\delta-\delta}Cl$ --- $F^{+\delta-\delta}H$  in FCl-FH. The PL charge redistribution as well as the PL energy is larger for ClF-HF than for FCl-FH. CT transfers electrons from the terminal atom of the electron donor to the terminal atom of the acceptor like Cl ← F in FCl-FH and F  $\rightarrow$  H in ClF-HF, causing a charge buildup in the intermolecular region. Table XVII indicates that MIX plays a very important role in redistribution of charge although its contribution to energy is totally negligible (Table XIV). MIX, which is in principle the coupling between CT and PL, apparently collaborates with PL and shifts the electrons, which have just been transferred by CT from the electron donor to the terminal atom of the electron acceptor, toward the further end of the acceptor. So, when CT + MIX is examined as a whole, the

Table XVI. Energy Components for FCI-FH, CIF-HF, and (HF)<sub>2</sub> as Functions of Intermolecular Separation (kcal/mol)

		FCI-FH <sup>a</sup>			CIF-HF <sup><i>b</i></sup>				$(HF)_2^{\nu}$
R, Å 2.474	2.774	2.808	3.074	1.7	1.917	2.0	2.3	1.873	
$\Delta E$	-2.2	-3.10	-3.11	-2.5	-4.1	-4.40	-4.36	-3.5	-7.4
ES	-5.8	-3.1	-2.9	-2.0	-5.9	-4.2	-3.8	-2.7	-7.3
EX	6.6	1.7	1.4	0.4	5.5	2.2	1.4	0.3	2.6
PL	-0.3	-0.1	-0.1	-0.1	-1.4	-0.8	-0.6	-0.3	-0.5
СТ	-2.9	-1.7	-1.5	-0.9	-2.7	-1.8	-1.5	-0.9	-2.1
MIX	0.2	0.1	0.1	0.0	0.3	0.1	0.1	0.0	-0.0

"Collinear FCIF and  $\angle$ CIFH = 115" assumed. R = r(CI-F)." Collinear CIFHF assumed. R = r(F-H)." Collinear HFHF assumed. R = r(F-H).

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**Figure 3.** Component electron density map for the anti-hydrogen bonded complex FC1-FH at r(C1-F) = 2.737 Å,  $\angle$ HFC1 = 141°, and  $\gamma = \pi - \angle$ FC1F = 0. The coordinate origin is F of FH, and plotting is made for the molecular plane. See Figure 1 for other details.

electron appears to migrate from the donor to the further end of the acceptor.<sup>10</sup> The charge decomposition as well as the energy decomposition (Table XIV) analyses confirm that the hydrogen bonded complex CIF-HF is more strongly interacting, i.e., its individual energy and charge components are larger than those of the anti-hydrogen bonded complex FCl-FH, even though the total interaction energy is comparable between the two complexes.

Table XVIII shows the change in the dipole moment and its components at the experimental geometry for FCl-FH. There is about 10% (0.3D) enhancement of the dipole moment upon complex formation. Though the absolute value of  $\mu$  is an overestimate (2.3 D experimental<sup>19</sup> vs. 3.6 D calculated with this basis set), one can still note that the enhancement is mainly due to PL, i.e., the induced dipole moment by the permanent multipoles, supplemented by CT and MIX. This trend is consistent with the charge redistribution analysis presented above.

### VI. (F<sub>2</sub>)<sub>2</sub>

As was briefly discussed in section I, the chlorine dimer  $(Cl_2)_2$  is established to be a polar complex with a dipole moment  $\geq 0.2$  D. Two models have been proposed as a possible structure of the polar complex. An "L" shaped structure is derived from the structure of the Cl<sub>2</sub> crystal. A "T" shaped structure is favored for the long-range quadrupole-quadrupole



Figure 4. Component electron density map for the hydrogen bonded complex CIF-HF at r(F-H) = 1.864 Å,  $\angle$ CIFH = 143°, and  $\angle$ FHF = 180°. The coordinate origin is H of HF, and a plotting is made for the molecular plane. See Figure 1 for other details.

interaction.<sup>20</sup> ( $F_2$ )<sub>2</sub> also may be a polar complex with a dipole moment of 0.1 D or larger.<sup>21</sup>

(A) SCF Geometry Optimization. We examined various geometries of  $(F_2)_2$  complexes employing, as a first approximation, the SCF scheme. The F-F distance of the fluorine molecule was taken to be 1.435 Å<sup>29</sup> in this section and kept unchanged throughout the complex calculation. Geometries of  $(F_2)_2$  studied are schematically shown in Figure 5. In all the models the four atoms are assumed to be coplanar ( $C_s$  symmetry) and F<sub>b</sub>, F<sub>c</sub>, and F<sub>d</sub> are collinear. Models I, III, and II have F<sub>c</sub>F<sub>d</sub> perpendicular to the F<sub>a</sub>F<sub>b</sub> axis at the midpoint of the F<sub>a</sub>F<sub>b</sub> bond, on the atom F<sub>b</sub>, and at the midpoint of I and III, respectively. The intermolecular distance R is defined as the distance between F<sub>c</sub> and the F<sub>a</sub>F<sub>b</sub> axis. All other models have F<sub>c</sub>F<sub>d</sub> rotated sequentially by 15° along the circular arc of which F<sub>b</sub> is the center, with R being the F<sub>b</sub>-F<sub>c</sub> distance. Figure 6

Table XVII. Gross Atomic Electron Population of Isolated Molecules and Its Component Changes for the Complexes $HF^{a,b}$	FCI-FH and CIF

	FCI		FH	(+)	
	Fa	Cl	F <sub>b</sub>	Н	$FCI \stackrel{(+)}{\underset{(-)}{\longleftarrow}} FH$
Isolated molecules	9.3950	16.6050	9.4786	d.5214	
Total change	0.0274	-0.0165	0.0019	-0.0128	-0.0109
EX	0.0009	-0.0009	-0.0003	0.0003	010105
PL	0.0199	-0.0199	0.0127	-0.0127	
СТ	0.0004	0.0108	-0.0101	-0.0011	-0.0112
MIX	0.0066	-0.0063	-0.0004	0.0007	0.0003
		ClF		HF	
	Cl	F <sub>a</sub>	H	F <sub>b</sub>	$CIF \stackrel{(+)}{\underset{(-)}{\longleftarrow}} HF$
Isolated molecules	16.6050	9.3950	0.5214	9.4786	
Total change	-0.0538	0.0344	-0.0175	0.0369	0.0194
EX	0.0005	-0.0005	-0.0032	0.0032	
PL	-0.0508	0.0508	-0.0128	0.0128	
СТ	-0.0035	-0.0147	0.0217	-0.0035	0.0182
MIX	-0.0001	-0.0011	-0.0231	0.0243	0.0012
	-0.0001	-0.0011	0.0231	0.0245	0.0012

<sup>*a*</sup> At the calculated equilibrium geometries. FCI-FH: r(CI-F) = 2.737 Å,  $\angle CIFH = 141^{\circ}$  and collinear FCIF. CIF-HF: r(F-H) = 1.864 Å,  $\angle CIFH = 143^{\circ}$  and collinear FHF. <sup>*b*</sup> For sign conventions, see Table 11.

**Table XVIII.** The Dipole Moment Change  $\Delta \mu$  and Its Components in D for the Anti-Hydrogen Bonded Complex FCl-FH at Experimental Geometry<sup>*a*</sup>

	$\mu_x^{b}$	$\mu_{\tau}^{c}$	μ
Monomers <sup>d</sup>	2.07	2.55	3.28
$\Delta \mu^{e}$	0.02	0.38	0.32
$\Delta \mu_{FX}$	-0.00	0.02	0.01
$\Delta \mu_{\rm PL}$	0.02	0.20	0.17
$\Delta \mu_{\rm CT}$	0.00	0.11	0.08
$\Delta \mu_{M1X}$	-0.00	0.05	0.04

<sup>*a*</sup> r(Cl-F<sub>b</sub>) = 2.774 Å and ∠ClF<sub>b</sub>H = 115°. γ = 0 is assumed in 10. <sup>*b*</sup> Perpendicular to the F<sub>a</sub>ClF<sub>b</sub> axis. A positive value corresponds to the polarity <sup>+</sup>H(F<sub>a</sub>ClF<sub>b</sub>)<sup>-</sup>. <sup>*c*</sup> Parallel to the F<sub>a</sub>ClF<sub>b</sub> axis. A positive value corresponds to the polarity <sup>-</sup>F<sub>a</sub>ClF<sub>b</sub>H<sup>+</sup>. <sup>*d*</sup> The vector sum of the calculated monomer dipoles. <sup>*e*</sup> The total change of dipole moment upon complex formation:  $\Delta \mu = \mu$ (complex) –  $\mu$ (monomers).



Figure 5. Assumed models 1-1X for  $(F_2)_2$ . All atoms are in a plane. In models 1-11,  $F_cF_d$  is perpendicular to  $F_aF_b$  with *R* being the distance between  $F_c$  and the bond  $F_aF_b$ . In models 111 to 1X,  $F_b$ ,  $F_c$ , and  $F_d$  are collinear with *R* being the  $F_bF_c$  distance.

shows  $\Delta E_{SCF}$  for R = 2.7 and 3.0 Å. The smaller R is chosen as a sum of the van der Waals radius (1.35 Å) of the F atoms.<sup>37</sup> A calculation at a smaller R = 2.55 Å for model V indicates that the complex is repulsive, suggesting that R = 2.7 Å can be taken as the most stable geometry. Another calculation at R = 3.3 Å for model III indicates that R = 3.0 Å is the best distance for this model. Additional calculations (not shown)



Figure 6. The \$CF interaction energy  $\Delta E_{\text{SCF}}$  for models in Figure 5. Two R's are 2.7 and 3.0 Å, respectively, where X's indicate the positions of the F<sub>c</sub> atom. Exceptions are a point at R = 2.55 Å for V and another at R = 3.3 Å for 111. The energies are in kcal/mol.

were also carried out for several structures in which  $F_d$  is moved out of the plane of the complex (non-planar models) or  $F_d$  is kept within the plane but is made nonlinear with respect to the  $F_bF_c$  axis (nonlinear models). In all cases the complex formed is much less stable than the corresponding coplanar, collinear models. We may conclude, therefore, that the most stable geometry within  $\Delta E_{SCF}$  is an open L-shaped structure, model V with R = 2.7 Å. The stability of the complex due to  $\Delta E_{SCF}$ is extremely small.

(B) Dispersion Energy. Since the contribution of  $\Delta E_{SCF}$  is so small, the dispersion energy DISP may be equally as important as the  $\Delta E_{SCF}$  contribution. DISP, estimated by a second-order perturbation method, is shown in Figure 7. The DISP stabilization increases as the angle between the two fluorine molecules increases, reaching a maximum when  $F_aF_b$ and  $F_cF_d$  are collinear. This trend seems to be reasonable as will be discussed shortly. Though the contribution of DISP increases as *R* becomes smaller, the steep repulsion due to  $\Delta E_{SCF}$  seems to keep the equilibrium *R* around 2.7 Å, as is seen for model V. Since the criteria of reliability of DISP

**Table XIX.** Energy Components (kcal/mol), Dipole Moment (D), and Atomic Population Change of the  $(F_2)_2$  Complex for Various Models at R = 2.7 Å

	Model <sup>a</sup>						
	<u>l</u>	111	v	V11	IX		
		Energy					
$\Delta E$	-0.20	-0.23	-0.38	-0.42	-0.43		
DISP	-0.13	-0.11	-0.21	-0.31	-0.36		
$\Delta E_{SCF}$	-0.07	-0.12	-0.17	-0.11	-0.07		
ES	0.01	-0.06	-0.08	0.03	0.09		
EX	0.39	0.38	0.33	0.26	0.23		
PL	-0.00	-0.00	-0.00	-0.00	-0.00		
СТ	-0.46	-0.46	-0.42	-0.43	0.29		
MIX	-0.40	0.03 -0.42		0.03	-0.38		
		Dipole Moment					
#SCF	0.021	0.033	0.040	0.018	0		
μ <sub>PL</sub>	0.000	0.014	0.021	0.013	0		
$\mu_{CT+EX+MIX}$	0.021	0.019	0.019	0.005	0		
	Atom	ic Population Chan	ge <sup>b</sup>				
Fa	-0.0005	-0.0023	-0.0027	-0.0024	-0.0023		
F <sub>b</sub>	-0.0005	0.0010	0.0015	0.0020	0.0023		
Fe	0.0001	-0.0006	-0.0007	0.0011	0.0023		
F <sub>d</sub>	0.0009	0.0018	0.0018	-0.0007	-0.0023		

" As defined in Figure 5. <sup>b</sup> Positive and negative values indicate an increase and a decrease, respectively, of electron population upon complex formation.

calculated in the present procedure are not as well established as those of  $\Delta E_{\rm SCF}$ , its absolute magnitude should not be taken too seriously. Due to the importance of DISP the total stabilization  $\Delta E$  calculated as a simple sum  $\Delta E_{\rm SCF}$  + DISP, Table XIX, yields a linear equilibrium structure. A more quantitative balance in reliability between  $\Delta E_{\rm SCF}$  and DISP is required to make a sensible prediction of geometry.

DISP's preference for the linear geometry can be explained by examining the leading term in the perturbation sum, eq 3. While the numerator depends strongly on the mutual orientation as well as the distance R between the two monomers, the denominator in the present perturbation method is constant regardless of the geometry. A discriminatively large contribution for the linear geometry comes from the  $(7_A 10_A | 7_B 10_B)$ integral, i.e., the interaction between the  $7 \rightarrow 10$  transitions of the monomers, where the seventh MO is an occupied  $\sigma_g$  MO and the tenth MO is the lowest vacant  $\sigma_u^*$  MO. This transition, whose moment is parallel to the  $F_2$  molecular axis, yields the largest contribution to DISP when the two monomers are collinear. Since the numerator of eq 3 is the square of  $\langle i_{A}$  $j_A | k_B l_B \rangle$ , the term gives a  $\cos^2 \theta$ -like angular dependence where  $\theta = \angle F_a F_b F_c$ .

(C) Energy Decomposition Analysis. The energy decomposition analysis of  $\Delta E_{SCF}$  is also given in Table XIX. ES is merely a small contributor to the stabilization, though its angular dependency is the most pronounced. The magnitude of ES in Table XIX is consistent with an order-of-magnitude estimate based on the quadrupole-quadrupole interaction  $E_{\theta\theta}$ ; by assuming the quadrupole moment of  $F_2 = 1 \times 10^{-26}$  esu cm<sup>2</sup>, R = 2.7 + 0.5 = 3.2 Å, one obtains  $E_{\theta\theta}$  ca. -0.1 kcal/mol. The angular dependence, however, is different from what is expected from a consideration of only  $E_{\theta\theta}$ , which favors the "T" shape, model I. A tempting interpretation of ES as well as EX is based on the electron distribution of F2, which is more dense (or more negative) to the direction of the  $\pi$  orbitals than the  $\sigma$  orbitals (the molecular axis). The linear model IX, which has a  $\sigma$ - $\sigma$  or positive-positive contact of electron clouds, is very favorable for EX but is unfavorable for ES. In perpendicular models I and III there are two factors: an  $F_cF_b$  positive  $\sigma$ - $F_aF_b$ negative  $\pi$  contact which has a favorable ES and an  $F_cF_d$ negative  $\pi$ -F<sub>a</sub>F<sub>b</sub> negative  $\pi$  contact which is undesirable for



Figure 7. The dispersion energy DISP for models in Figure 5. For other details see Figure 6.

both ES and EX. A balance of these factors apparently favors the open L geometry of model V.

The absolute value of CT is rather small yet is the largest component for  $(F_2)_2$ . Surprisingly its magnitude depends only weakly on the angle. For the T-shaped model I  $\pi \rightarrow \sigma^*$  and  $\pi \rightarrow \pi^*$  type overlap are the dominant contributions to CT.



For the linear model IX, another type of overlap,  $\sigma \rightarrow \sigma^*$ , is the dominant contribution.



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Table XX. Energy Components (kcal/mol) at the Optimized Intermolecular Separation  $R_e$  and Qualitative Classification of EDA Complexes with the 4-31G Basis Set

Donor-Acceptor	Туре	R <sub>e</sub> , A	$\Delta E_{\rm SCF}$	ES	EX	PL	СТ	MIX	Classification <sup>a</sup>
$H_3N-BF_3^b$	$n-\sigma^*$	1.60	-71.5	-142.3	136.3	-42.7	-52.7	29.9	Strong ES
H <sub>3</sub> N-BH <sub>3</sub> b	$n-\sigma^*$	1.70	-44.7	-92.9	86.9	-17.2	-27.1	5.6	Strong ES
$OC-BH_3b$	$\sigma - \sigma^*$	1.63	-28.5	-60.9	98.9	-61.8	-68.3	63.6	Strong CT-PL-ES
5	$\pi^* - \pi$								-
H <sub>3</sub> N-ClF	$n - \sigma^*$	2.72	-8.2	-11.2	7.4	-1.1	-3.6	0.2	Intermediate ES
$H_{2}O-OC(CN)_{2}c$	$n-\pi^*$	2.70	-8.0	-9.7	4.4	-1.0	-1.8	3d	Intermediate ES
HF-CIF	$n - \sigma^*$	2.74	-3.4	-3.6	1.8	-0.2	-1.4	0.1	Weak ES
$H_3N-Cl_2$	$n - \sigma^*$	2.93 <sup>e</sup>	-2.9	-4.0	3.9	-0.8	-2.3	0.3	Weak ES-CT
Benzene $-OC(CN), f, g$	$\pi - \pi^*$	3.6-3.8							Weak ES-DISP
$H_3N-F_2$	$n - \sigma^*$	3.00	-1.1	-0.8	0.6	-0.3	-0.6	0.0	Weak ES-CT
$H_{2}CO-F_{3}$	$n-\sigma^*$	2.91	-0.7	-0.4	0.3	-0.1	-0.5	0.0	Weak CT-ES-DISP
$H_{2}CO - C_{2}H_{4}f$	$\pi - \pi$	3.75	-0.7	-0.5	0.4	-0.1	-0.5	5d	Weak CT-ES
F <sub>2</sub> -F <sub>2</sub>	$\pi - \sigma^*$	2.7	-0.2	-0.1	0.3	0.0	-0.4	0.0	Weak DISP-CT

<sup>*a*</sup> Qualitative classification based on the predominant contributions which are 50% or more of the largest contribution. See text. <sup>*b*</sup> Reference 14. <sup>*c*</sup> Reference 12. <sup>*d*</sup> CT + M1X. <sup>*e*</sup> Not optimized. <sup>*f*</sup> Reference 13. <sup>*s*</sup> Only STO-3G calculations have been carried out.

Apparently the contributions are of comparable magnitude, giving rise to a small overall CT angular dependence.

(D) Dipole Moment. As a measure of the polarity of this complex, the dipole moment  $\mu$  should be examined. The SCF dipole moment and its components are shown in Table XIX. It is interesting to note that the model V of maximum dipole moment coincides with that of the best  $\Delta E_{SCF}$ . Components of the dipole moment and atomic population changes due to complex formation, also shown in Table XIX, suggest a rather complicated motion of electrons (mainly due to PL and CT) is taking place as the geometry changes from I through III to IX. The contribution of the dispersion interaction to the dipole moment is calculated from the first-order dispersion-perturbed wave function  $\psi$ .

$$\psi = A_0 B_0 - \sum_{i}^{\text{occ}} \sum_{k}^{\text{vac}} \sum_{\nu}^{\text{occ}} \frac{\sum_{i}^{\text{vac}} \left\langle A_0 B_0 \right| H' | A_{i \to k} B_{\mu \to \nu} \right\rangle}{E_{i_A \to k_A, \mu_B \to \nu_B} - E_0} \times A_{i \to k} B_{\mu \to \nu} \quad (4)$$

where  $A_0B_0$  is the Hartree product of the Hartree-Fock wave functions of the ground state of the molecule A and B,  $A_{i\rightarrow k}B_{\mu\rightarrow\nu}$  is the Hartree product of the wave functions for the singly excited states of A and B.<sup>13</sup> The calculated dispersion contribution to the dipole moment is found to be negligible (<0.001 D).

The largest calculated dipole moment  $\mu_{\rm SCF} \sim 0.04$  D (model V) is substantially smaller than the experimental estimate (>0.1 D). The origin of this discrepancy is not obvious. It is possible, though unlikely, that the calculated  $R_e$  is too large; if  $R_e$  is smaller than 2.7 Å by 0.2–0.3 Å, the calculated  $\mu_{\rm SCF}$  becomes comparable to the experimental threshold and the optimum geometry by  $\Delta E_{\rm SCF}$  + DISP would be similar to model V. It may also be dependent on the basis set or influenced by the correlation effect.<sup>38</sup> We did not test either of these conjectures.

#### VII. Discussion and Conclusions

Energy decomposition results employing the 4-31G basis set at calculated equilibrium geometries of each of the EDA complexes examined in this paper as well as in the previous papers of our series are summarized in Table XX. Very qualitative classifications have also been given. In those cases in which truncated potential energy calculations have been carried out, the classification is based on what components are required to maintain the binding characteristics of the complex. When this has not been done, those contributions whose magnitude was greater than 50% of that of the largest component were assumed to be essential to the binding. Since 4-31G set exaggerates the ES contribution, the corresponding percentage for a calculation with a larger basis set would be about 70%. Anyway, the classifications are meant to be only a qualitative guide to the nature of complex binding and should not be taken as an absolute, definitive categorization. For instance HF-ClF and H<sub>3</sub>N-ClF have been tentatively labeled as "ES complexes" in Table XX, one may equally as well call them "ES-CT", or still better "ES > CT complexes".

In Table XX, certain trends in the origin of stabilization among varieties of EDA complexes are evident. Three classes are recognized for  $n-\sigma^*$  type complexes. A polar-polar complex is the strongest and is dominated by a large ES contribution even though CT and PL are not negligible. OC-BH<sub>3</sub> is an exceptional, strong CT-PL-ES complex, which arises from CO's duality in the CT interaction, acting both as a  $\sigma$ donor and a  $\pi^*$  acceptor. A polar-nonpolar complex is intermediate to weak, with both ES and CT being major contributions. A nonpolar-nonpolar complex is very weak, with both DISP and CT contributing to the stabilization. A polar n donor- $\pi^*$  acceptor complex seems to be a weak to intermediate ES complex, whereas a  $\pi$  donor- $\pi^*$  acceptor looks to be of ES-DISP type. Further detailed elaboration of the classification of EDA complexes will be deferred to subsequent papers.

For  $H_3N$ - and  $H_2CO$ -halogen complexes studied in the paper, the following conclusions can be made in addition to those included in Table XX.

(i) A deviation of H<sub>3</sub>N-halogen complexes from the  $C_{3r}$  geometry results in destabilization due to ES and EX, which may be explained in terms of difference in electron distribution of the halogens in the  $\pi$  and  $\sigma$  directions.

(ii) All the components of the  $Cl_2$  complex are larger than the corresponding components for the  $F_2$  complex. This may be interpreted as the result of the difference in the size of electron distribution.

(iii) The N-methyl substituent effect is small due to a cancellation of the EX and CT components. This is compared with a small substituent effect for  $H_3N-BH_3$ , which is the result of PL-EX cancellation, and a large effect for  $H_3N-H^+$ , which is due to PL.

For FCl-FH anti-hydrogen bonded and ClF-HF hydrogen bonded complexes, the following additional conclusions can be drawn.

(i) The energies of the two forms appear to be very similar: the 4-31G set prefers ClF-HF, while the larger 4-31G\*\* set favors FCl-FH.

(ii) The calculated geometry of FCl-FH is in good agreement with experiment.

(iii) The geometry of ClF-HF is predicted to be:  $r(F-F) \sim 2.86 \text{ Å}, \angle \text{ClF-H} \sim 130^\circ$ , and  $\angle \text{FHF} \sim 180^\circ$ .

(iv) The deviation of  $F_a$  from the collinearity in  $F_aCl-F_bH$  is not favorable due to EX, supplemented by ES or CT de-

pending on the mode of deviation. This may be explained in terms of differences in the electron distribution in ClF between  $\pi$  and  $\sigma$  directions.

(v) The major difference in the energy components between FCl-FH and ClF-HF is EX.

For  $(F_2)_2$  the additional conclusions are:

(i)  $\Delta E_{SCF}$  favors an "open L" shape structure with an angle of 120°, the shortest intermolecular F-F separation being 2.7 A. This shape is a result of different competing overlaps between occupied and vacant MO's.

(ii) DISP prefers a linear structure, which gives a favorable alignment of  $\sigma - \sigma^*$  transition dipoles.

(iii) CT is the largest source of  $\Delta E_{SCF}$ , whose angular dependence is controlled by a balance of different modes of MO overlaps.

(iv) The calculated dipole moment is  $\sim 0.04$  D, smaller than the experimental estimate.

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